

# ALNUTH

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## ALgebraic NUmber Theory and an interface to PARI/GP

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*Note:* PARI/GP is **not** part of this package. It can be obtained from <https://pari.math.u-bordeaux.fr/>

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# 1

# Introduction

A number field is a finite extension of the field of rational numbers. **Alnuth** provides various methods to compute with number fields which are given by a defining polynomial or by generators. For background on number fields we refer to [ST79].

Some of the methods provided in this package are written in **GAP** code. The other part of the methods is imported from the Computer Algebra System **PARI/GP** [PAR11]. Hence this package contains some **GAP** functions and an interface to some functions in the computer algebra system **PARI/GP**. Therefore one has to have **PARI/GP** installed to use the full functionality of **Alnuth**.

We note that only a very small part of the functions available in **PARI/GP** are linked to **GAP** and **PARI/GP** provides many more methods for computations in number fields.

The main methods included in **Alnuth** are: creating a number field, computing its maximal order (using **PARI/GP**), computing its unit group (using **PARI/GP**) and a presentation of this unit group, computing the elements of a given norm of the number field (using **PARI/GP**), determining a presentation for a finitely generated multiplicative subgroup (using **PARI/GP**), and factoring polynomials defined over number fields (using **PARI/GP**). For background on algorithms for number fields we refer to [Poh93], [PZ89] and [Coh93].

The functions provided by **Alnuth** are introduced in the following chapter. Then an example application is outlined. In the final chapter of this manual the installation of the package and configuration of the interface, including hints on the installation of **PARI/GP**, are described.

## 1.1 Acknowledgements

To begin with we are very grateful for all the feedback by users of former versions of **Alnuth**.

We thank Bill Allombert who wrote the **GP** code for the interface to **PARI/GP** and who was extremely helpful in the transition from **KANT** to **PARI/GP**.

For feedback on the development version, including a code patch, we are much obliged to Max Horn.

The second author acknowledges the financial support at CAUL within the projects PTDC/MAT/101993/2008 and ISFL-1-143, financed by FEDER and FCT, in the development of Version 3 of **Alnuth**.

## 1.2 License

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# 2

# Methods for number fields

An algebraic number field is a finite-dimensional extension of the rational numbers  $\mathbb{Q}$ . Such a number field has a primitive element and it can be defined by the minimal polynomial of this primitive element. Another important way to define an algebraic number field is by a set of rational matrices which generate a number field.

## 2.1 Creation of number fields

We provide functions to create number fields defined by rational matrices or by rational polynomials.

- 1 ► `FieldByMatricesNC( matrices )`
  - `FieldByMatrices( matrices )`

Creates a field generated by the rational matrices *matrices*. In the faster NC version, the function assumes that the input generates a field and there are no checks on this performed.

- 2 ► `FieldByMatrixBasisNC( matrices )`
  - `FieldByMatrixBasis( matrices )`

Creates a field with basis *matrices*. The list *matrices* must consist of rational matrices which form a basis for a number field. In the faster NC version, the function assumes that the input is a matrix basis for a field and no checks are performed.

- 3 ► `FieldByPolynomialNC( polynomial )`
  - `FieldByPolynomial( polynomial )`

Creates a field defined by *polynomial*. The polynomial *polynomial* must be an irreducible rational polynomial. In the faster NC version, no checks on the input are performed.

## 2.2 Methods for number fields

We outline a number of functions for number fields.

- 1 ► `PrimitiveElement( F )`
  - `DefiningPolynomial( F )`

Computes a primitive element and a defining polynomial for the given number field. The defining polynomial is the minimal polynomial of the primitive element. Since *F* contains various primitive elements, `PrimitiveElement` tries to find a primitive element which has a minimal polynomial with small coefficients. Via the global variable `PRIM_TEST` the user can decide how many primitive elements will be compared. The default value is 20.

- 2 ► `IsPrimitiveElementOfNumberField( F, a )`

Checks if the given element generates the field.

- 3 ► `DegreeOverPrimeField( F )`

Returns the degree of *F* over the rationals.

- 4 ▶ `EquationOrderBasis( F )`
- ▶ `MaximalOrderBasis( F )`
- ▶ `IsIntegerOfNumberField( F, k )`

These functions return bases for the equation order or the maximal order of the number field  $F$ . Also, they allow to check if a given element is an integer in the given number field.

- 5 ▶ `UnitGroup( F )`

determines the unit group of  $F$ .

Recall that the unit group of  $F$  is a finitely generated abelian group. The function `IsomorphismPcpGroup` from the `Polycyclic` [EHN11] package gives an isomorphism to a pcg group which can be used for various computations with the unit group.

- 6 ▶ `IsUnitOfNumberField( F, k )`

checks whether the element  $k$  is a unit in  $F$ .

- 7 ▶ `ExponentsOfUnits( F, elms )`

This function determines the exponent vectors of the elements in  $elms$  with respect to the generators of the unit group of  $F$ . If the unit group of  $F$  is not known, then the function computes this unit group also.

- 8 ▶ `IsCyclotomicField( F )`

Check whether  $F$  is cyclotomic.

- 9 ▶ `NormCosetsOfNumberField( F, norm )`

Returns a description for the set of all elements of norm  $norm$  in  $F$ . These elements can be written as a finite union of cosets of the unit group of  $F$ . The function returns coset representatives for these cosets.

## 2.3 Presentations of multiplicative subgroups

Suppose that a finite number of invertible elements of a number field are given. Then these elements generate a finitely generated abelian group. However, it is a non-trivial task to provide a presentation for this abelian group. The most useful representation for such groups is as pcg group.

- 1 ▶ `PcpPresentationOfMultiplicativeSubgroup( F, elms )`
- ▶ `IsomorphismPcpGroup( F, elms )`

Determine a pcg presentation for the multiplicative group of  $F \setminus \{0\}$  generated by  $elms$  and an isomorphism on this presentation. Note, that the method `IsomorphismPcpGroup` is defined in the `Polycyclic` package [EHN11]. We refer to the manual of this package for further background.

In the determination of the Pcp-presentation of a multiplicative subgroup generated by  $elms$  the relations between the elements in  $elms$  play an important role. Let  $elms = \{e_1, \dots, e_l\}$  be a finite subset of a field  $F$ . The relation lattice for  $elms$  is

$$rl(elms) := \left\{ (h_1, \dots, h_l) \in \mathbb{Z}^l \mid e_1^{h_1} \cdots e_l^{h_l} = 1 \right\}.$$

- 2 ▶ `RelationLattice( F, elms )`

Determines a generating set for the relation lattice of the field elements  $elms$ .

## 2.4 Methods to compute with subgroups of the unit group

### 1 ► RelationLatticeOfUnits( *F*, *elms* )

Determines a basis for the relation lattice of the units *elms* in triangularized form. Note that this method is more efficient than the method `RelationLattice`.

### 2 ► IntersectionOfUnitSubgroups( *F*, *gen1*, *gen2* )

The lists *gen1* and *gen2* are supposed to generate two subgroups  $U_1$  and  $U_2$  of the unit group of  $F$ . This function determines the intersection of  $U_1$  with  $U_2$ . The result is returned as a list of vectors generating the lattice  $\{e \in \mathbb{Z}^n \mid g_1^{e_1} \cdots g_n^{e_n} \in U_2\}$  for  $gen1 = [g_1, \dots, g_n]$ .

For efficiency reasons this function does not check the input and it may return wrong results if the input generators do not fulfil the requirements.

## 2.5 Factorisation of polynomials over a number field

### 1 ► FactorsPolynomialAlgExt( *F*, *pol* )

embeds the rational polynomial *pol* into the polynomial ring over the number field  $F$ , which has to be constructed by `FieldByPolynomial` or `AlgebraicExtension`, and returns the factorization of the embedded polynomial. By default *a* denotes the primitive element of the field one can obtain from `PrimitiveElement( $F$ )`, that is, a root of the defining polynomial of  $F$ .

### 2 ► FactorsPolynomialPari( *pol* )

takes a polynomial *pol* defined over an algebraic extension of the Rationals and factors it using PARI/GP.

```
gap> x := Indeterminate( Rationals, "x" );;
gap> pol := 2*x^7+2*x^5+8*x^4+8*x^2;
2*x^7+2*x^5+8*x^4+8*x^2
gap> L := FieldByPolynomial( x^3-4 );
<algebraic extension over the Rationals of degree 3>
gap> y := Indeterminate( L, "y" );;
gap> FactorsPolynomialAlgExt( L, pol );
[ !2*y, y, y+(a), y^2+!1, y^2+((-1*a))*y+(a^2) ]
gap> FactorsPolynomialPari( last[5] );
[ y^2+((-1*a))*y+(a^2) ]
gap>
```

## 2.6 Examples

### 1 ► ExampleMatField( *l* )

This function returns some examples of fields generated by matrices. There are 9 such example fields provided and they can be obtained by assigning the input *l* to an integer between 1 and 9. Some of the properties of the examples are summarized in the following table.

	degree over $\mathbb{Q}$	number of generators	dim. of generators
<code>ExampleMatField(1)</code>	4	4	4
<code>ExampleMatField(2)</code>	4	4	4
<code>ExampleMatField(3)</code>	4	4	4
<code>ExampleMatField(4)</code>	4	13	4
<code>ExampleMatField(5)</code>	4	13	4
<code>ExampleMatField(6)</code>	4	7	4
<code>ExampleMatField(7)</code>	4	18	4
<code>ExampleMatField(8)</code>	4	13	4
<code>ExampleMatField(9)</code>	4	7	4

# 3

# An example application

In this section we outline two example computations with the functions of the previous chapter. The first example uses number fields defined by matrices and the second example considers number fields defined by a polynomial.

## 3.1 Number fields defined by matrices

```
gap> m1 := [ [ 1, 0, 0, -7 ],
             [ 7, 1, 0, -7 ],
             [ 0, 7, 1, -7 ],
             [ 0, 0, 7, -6 ] ];;

gap> m2 := [ [ 0, 0, -13, 14 ],
             [ -1, 0, -13, 1 ],
             [ 13, -1, -13, 1 ],
             [ 0, 13, -14, 1 ] ];;

gap> F := FieldByMatricesNC( [m1, m2] );
<rational matrix field of unknown degree>

gap> DegreeOverPrimeField(F);
4
gap> PrimitiveElement(F);
[ [ -1, 1, 1, 0 ], [ -2, 0, 2, 1 ], [ -2, -1, 1, 2 ], [ -1, -1, 0, 1 ] ]

gap> Basis(F);
Basis( <rational matrix field of degree 4>,
[ [ [ 1, 0, 0, 0 ], [ 0, 1, 0, 0 ], [ 0, 0, 1, 0 ], [ 0, 0, 0, 1 ] ],
  [ [ 0, 1, 0, 0 ], [ -1, 1, 1, 0 ], [ -1, 0, 1, 1 ], [ -1, 0, 0, 1 ] ],
  [ [ 0, 0, 1, 0 ], [ -1, 0, 1, 1 ], [ -1, -1, 1, 1 ], [ 0, -1, 0, 1 ] ],
  [ [ 0, 0, 0, 1 ], [ -1, 0, 0, 1 ], [ 0, -1, 0, 1 ], [ 0, 0, -1, 1 ] ] ] )

gap> MaximalOrderBasis(F);
Basis( <rational matrix field of degree 4>,
[ [ [ 1, 0, 0, 0 ], [ 0, 1, 0, 0 ], [ 0, 0, 1, 0 ], [ 0, 0, 0, 1 ] ],
  [ [ -1, 1, 1, 0 ], [ -2, 0, 2, 1 ], [ -2, -1, 1, 2 ], [ -1, -1, 0, 1 ] ],
  [ [ -3, -2, 2, 3 ], [ -3, -5, 0, 5 ], [ 0, -5, -3, 3 ], [ 2, -2, -3, 0 ] ],
  [ [ -1, -1, 0, 1 ], [ 0, -2, -1, 1 ], [ 1, -1, -2, 0 ], [ 1, 0, -1, -1 ] ]
] )

gap> U := UnitGroup(F);
<matrix group with 2 generators>

gap> u := GeneratorsOfGroup( U );;
```

```

gap> nat := IsomorphismPcpGroup(U);;
gap> H := Image(nat);
Pcp-group with orders [ 10, 0 ]
gap> ImageElm( nat, u[1] );
g1
gap> ImageElm( nat, u[2] );
g2
gap> ImageElm( nat, u[1]*u[2] );
g1*g2
gap> u[1] = PreImagesRepresentative(nat, GeneratorsOfGroup(H)[1] );
true

```

## 3.2 Number fields defined by a polynomial

```

gap> g := UnivariatePolynomial( Rationals, [ 16, 64, -28, -4, 1 ] );
x_1^4-4*x_1^3-28*x_1^2+64*x_1+16

gap> F := FieldByPolynomialNC(g);
<algebraic extension over the Rationals of degree 4>
gap> PrimitiveElement(F);
a
gap> MaximalOrderBasis(F);
Basis( <algebraic extension over the Rationals of degree 4>,
[ !1, 1/2*a, 1/4*a^2, 1/56*a^3+1/14*a^2+1/14*a-2/7 ] )

gap> U := UnitGroup(F);
<group with 4 generators>

gap> natU := IsomorphismPcpGroup(U);;
gap> elms := List( [1..10], x-> Random(F) );;

gap> PcpPresentationOfMultiplicativeSubgroup( F, elms );
Pcp-group with orders [ 0, 0, 0, 0, 0, 0, 0, 0, 0, 0 ]

gap> isom := IsomorphismPcpGroup( F, elms );;
gap> y := RandomGroupElement( elms );;
gap> z := ImageElm( isom, y );;
gap> y = PreImagesRepresentative( isom, z );
true

gap> FactorsPolynomialAlgExt( F, g );
[ x_1+(-a), x_1+(a-2), x_1+(-1/7*a^3+3/7*a^2+31/7*a-40/7),
  x_1+(1/7*a^3-3/7*a^2-31/7*a+26/7) ]

```



# 4

# Installation

This package provides an interface between **GAP** and **PARI/GP**. **PARI/GP** itself is not part of this package. It has to be obtained and installed independently of this package. **Alnuth** works with **PARI/GP** Version 2.5 or higher.

## 4.1 Installing Alnuth

The package **Alnuth** is part of the standard distribution of **GAP** so that in most cases there is no need to install it separately. To use **Alnuth** you need to have **PARI/GP** installed. See the following section for information on **PARI/GP**.

In case you want to update **Alnuth** independently of your main **GAP** installation or if you are interested in an old version of **Alnuth** interfacing to **KANT/KASH** you can find all released versions of **Alnuth** in the form of gzipped tar-archives at

<https://github.com/gap-packages/alnuth/releases>

There are two ways of installing a **GAP** package. If you have permission to add files to the installation of **GAP** on your system you may install **Alnuth** into the `pkg` subdirectory of the **GAP** installation tree. Otherwise you may install **Alnuth** in a private `pkg` directory (for details see Subsections 76.1 and 9.2 in the **GAP** reference manual).

To install the latest version of **Alnuth** download one of the archives `alnuth.tar.gz`, move it to the directory `pkg` in which you want to install, and unpack the archive. If you are using the command line you can unpack with the command `tar xzf alnuth.tar.gz`.

## 4.2 Getting PARI/GP

Using **Alnuth** requires an installation of **PARI/GP** in Version 2.5 or higher. The software **PARI/GP** is freely available at

<https://pari.math.u-bordeaux.fr/>

Note that the place where **PARI/GP** is located in your system is independent of the place where **Alnuth** is installed.

### (a) Installing under Linux

In many Linux distributions **PARI/GP** can be installed via the software package manager, but this might sometimes be an older version which cannot be used together with **Alnuth**. (Starting **GP** from the command line with the option `--version-short` will show you the version number.)

If you install **PARI/GP** from source make sure you install with **GMP** support for better performance and complete the installation with `make install` so that you can start **GP** by just calling `gp` from the command line.

### (b) Installing under Windows

For Windows it is sufficient to get the basic **GP** binary which can be found at

<https://pari.math.u-bordeaux.fr/download.html>

### 4.3 Adjust the path of the executable for GP

This package needs to know where the executable for GP is. In the default setting *Alnuth* looks for an executable program named *gp* in the search paths of the system. More precisely, for a file *gp* inside one of the directories in the list returned by `DirectoriesSystemPrograms()` (called in a *GAP* session).

Under Linux the default setting should work with a standard installation of PARI/GP.

For the default setting to work under Windows the downloaded executable file, for example *gp-2-5-0.exe* has to be renamed to *gp.exe* and moved to one of the directories listed by `DirectoriesSystemPrograms()` (Ignore the leading *cygdrive* in each path name and note that the single letter specifies the drive, for example */cygdrive/c/Windows/* denotes the folder *Windows* on drive *C:*).

To check whether an executable of GP in Version 2.5 or higher is available with the default setting, you can use the function

#### 1 ► `PariVersion()`

which prints the version number, if the global variable `AL_EXECUTABLE` is bound to the file name of a GP executable.

If you cannot use the default setting for your purpose, you have two options to specify a new place and name for the GP executable.

If you are able to edit the file *defs.g* in the main directory of *Alnuth*, then you can change the line

```
BindGlobal("AL_EXECUTABLE", Filename(DirectoriesSystemPrograms(), "gp"));
```

to something like

```
BindGlobal("AL_EXECUTABLE", "/home/my/pari-2.5.0/gp");
```

under Linux or

```
BindGlobal("AL_EXECUTABLE", "/cygdrive/c/Users/my/Downloads/gp-2-5-0");
```

under Windows, where the second argument gives the path to the GP executable you want to use (Change the strings given above to reflect the actual path on your system.). Please note that in case of a new installation of *Alnuth* you will have to change *defs.g* again.

Alternatively you can also change your personal *gaprc* file (see the Subsection 3.2.2 in the *GAP* reference manual) for setting the variable `AL_EXECUTABLE` to a proper value. To do this add the appropriate line from above with the `BindGlobal` command to *gaprc*.

The third possibility is to change the path to the GP executable from within *GAP* using one of the following two functions. To do this you first have to load the package (see Section 4.4).

#### 2 ► `SetAlnuthExternalExecutable(path)`

adjusts the global variable `AL_EXECUTABLE` for the current *GAP* session. Depending on your installation of PARI/GP and your operating system the string *path* has to be either the command to start GP in a terminal (for example *gp*) or the complete path to the executable of GP (for example */cygwindrive/c/windows/gp*). The function returns *fail* if *path* does not execute GP in Version 2.5.0 or higher.

To make the change take effect for all of your *GAP* sessions, you can add `SetKantExecutable` with the path to the GP executable as argument to your personal *gaprc* file (see the Subsection 3.2.2 in the *GAP* reference manual).

If you want the change to affect all *GAP* session of all users of the *GAP* installation you can use the following function:

#### 3 ► `SetAlnuthExternalExecutablePermanently(path)`

does the same as `SetAlnuthExternalExecutable` and in addition tries to change the file *defs.g* accordingly in the currently loaded version of *Alnuth*. A warning is issued if there is no write access to *defs.g* from the current *GAP* session.

#### 4 ► `RestoreAlnuthExternalExecutable()`

tries to restore the original content of the file *defs.g* in the directory corresponding to the loaded version of *Alnuth*. The function returns *fail* if there is no write access to *defs.g* from the current *GAP* session.

## 4.4 Loading and testing the package

If Alnuth is not loaded when GAP is started you have to request it explicitly to use it. This is done by calling `LoadPackage("Alnuth");` in a GAP session. If Alnuth had not been loaded already a short banner will be displayed.

```
gap> LoadingPackage("alnuth");
Loading Alnuth 3.2.1 (Algebraic number theory and an interface to PARI/GP)
by Bjoern Assmann,
    Andreas Distler (a.distler@tu-bs.de), and
    Bettina Eick (http://www.iaa.tu-bs.de/beick).
maintained by:
    The GAP Team (support@gap-system.org).
Homepage: https://gap-packages.github.io/alnuth
Report issues at https://github.com/gap-packages/alnuth/issues
true
gap>
```

To load a certain version of Alnuth you can specify the version number as second argument in the call to `LoadPackage`. (See 77.2 Loading a GAP package in the reference manual or type `?LoadPackage` within a GAP session).

Once the package is loaded, it is possible to check the correct installation running a short test by calling `ReadPackage("Alnuth", "tst/testinstall.tst");`.

```
gap> ReadPackage("Alnuth", "tst/testinstall.g");
Architecture: aarch64-apple-darwin21.4.0-default64-kv8

testing: GAPROOT/pkg/alnuth/tst/ALNUTH.tst
        66 ms (33 ms GC) and 11.0MB allocated for GAPROOT/pkg/alnuth/tst/ALNUTH.tst
testing: GAPROOT/pkg/alnuth/tst/version.tst
        21 ms (21 ms GC) and 29.6KB allocated for GAPROOT/pkg/alnuth/tst/version.tst
-----
total          87 ms (54 ms GC) and 11.0MB allocated
              0 failures in 2 files

#I No errors detected while testing
gap>
```

The architecture, timings and memory usage will usually differ; other discrepancies in the output indicate some problem.

If the test suite runs into an error in the first part, which verifies the availability of PARI/GP, check your installation of PARI/GP and consult the last chapter of the documentation of Alnuth for more information.

If you find any bugs or have any suggestions or comments, we would very much appreciate it if you would let us know by submitting an issue at the Alnuth issue tracker on GitHub

<https://github.com/gap-packages/alnuth/issues>

or by writing an mail to [support@gap-system.org](mailto:support@gap-system.org).

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This index covers only this manual. A page number in *italics* refers to a whole section which is devoted to the indexed subject. Keywords are sorted with case and spaces ignored, e.g., “PermutationCharacter” comes before “permutation group”.

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